

Detector Array Evaluation
and
Figures of Merit

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This presentation will review the commonly used methods to evaluate the performance of a two-dimensional focal-plane array using charge transfer devices. Two figures of merit that attempt to combine quantum efficiency, read noise and dark-current generation into a single parameter are discussed. The figures of merit are suggested as possible alternatives to the D^* .

**DETECTOR ARRAY EVALUATION
AND
FIGURES OF MERIT**

STATE OF CONFUSION

- o **WHAT WE GET FROM MANUFACTURER**
- o **WHAT WE WANT**
- o **WHAT WE TEST FOR**

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**GENERIC PARAMETERS
QUOTED FROM MANUFACTURER**

- o **SIZE AND # OF PIXELS**
- o **D***
- o **D* HISTOGRAM**
- o **READ NOISE HISTOGRAM**
- o **DARK CURRENT HISTOGRAM**
- o **SATURATION LEVEL**
- o **RESPONSIVITY MAP**

D* PROBLEMS

- o **SMALL AREA DETECTORS ($D^* = \text{CONSTANT}$)**
- o **SPATIAL VARIATIONS ACROSS ARRAY**
- o **RADIANT "POWER" DEPENDENT FOR PHOTODETECTOR**
- o **$D^*(f)$ - NO $1/f$ CHARACTERISTIC (i.e., 0.5 Hz)**

SPECIFICATION OF CHOPPER FREQ.

- o **WAVELENGTH SPECIFICATION**

PARAMETERS WANTED BY USER

- o **SPATIAL AVERAGED QUANTUM EFF. vs WAVELENGTH**
- o **CONVERSION GAIN**
- o **SPATIAL AVERAGED DARK CURRENT vs INTEGRATION TIME FOR OPERATING TEMPERATURE**
- o **READ NOISE**
- o **DEFECTIVE PIXEL MAP**
- o **DYNAMIC RANGE**
- o **CROSSTALK**
- o **FILL FACTOR (DETECTOR AREA)**
- o **SATURATION LEVEL**

TEST/DATA COLLECTED

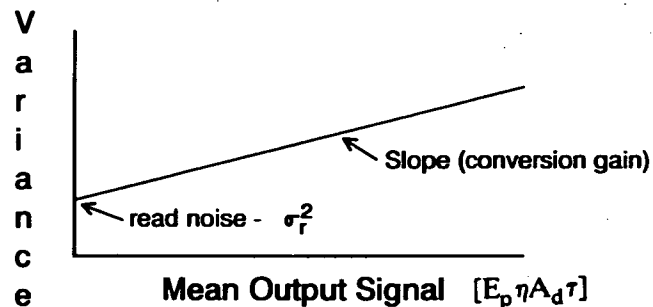
- o MEAN VARIANCE CURVE - σ_r
- o DARK CURRENT GENERATION - D_g
- o SIGNAL MEASURE FOR Q.E. OVER SPECTRAL BAND - η
- o EFFECTIVE DETECTOR AREA - A_d

PLOT SPATIAL MAPS OF:

- DARK CURRENT
- QUANTUM EFFICIENCY
- DEAD PIXELS

MEAN - VARIANCE CURVE

PLOT OF VARIANCE (NOISE²) VERSUS
THE MEAN IRRADIANCE (FLAT FIELD) ACROSS ARRAY



$$\sigma^2 = \sigma_r^2 + E_p \eta A_d \tau \text{ (electrons)}$$

COMPUTER PROCESSING

$E_p \propto \text{ADU}$ (ANALOG - DIGITAL UNITS IN COMPUTER)
SO UNITS CAN BE RELATED BETWEEN ADU'S AND
FLAT FIELD IRRADIANCE.

MEAN - VARIANCE IN PRACTICE

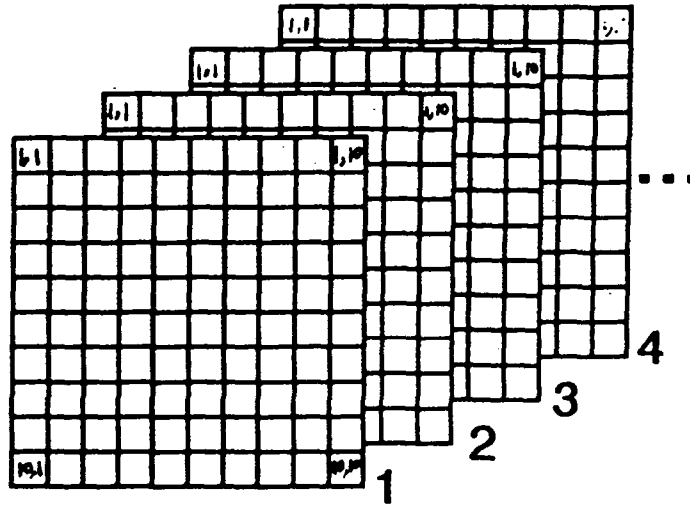
- o **TWO WAYS TO CHANGE MEAN IRRADIANCE ON ARRAY**
 - **VARY INTEGRATION TIME**
 - **VARY BLACKBODY TEMPERATURE, OR RANGE**

[NOT NECESSARILY EQUIVALENT]

IMPORTANCE OF DARK CURRENT

**WILL PHOTONS BE DETECTED IN INTEGRATION TIME,
OR WILL DARK GENERATED ELECTRONS DOMINATE
FOR PARTICULAR APPLICATION?**

DARK CURRENT TESTS



FOR VARIOUS INTEGRATION TIMES; ONE TAKES SEVERAL (i.e. 25) FRAMES OF DATA;

A. $\tau \cong 1 \text{ ms}$ (SHORTEST POSSIBLE)

$$\bar{P}_{ij} = \frac{1}{25} \sum_{K=1}^{25} P_{ij}(K) \quad ; \quad K \text{ is Time Index}$$

$$F_r = \{\bar{P}_{11}, \bar{P}_{12}, \bar{P}_{13} \dots \bar{P}_{ij}\} \quad \text{Average Dark Frame}$$

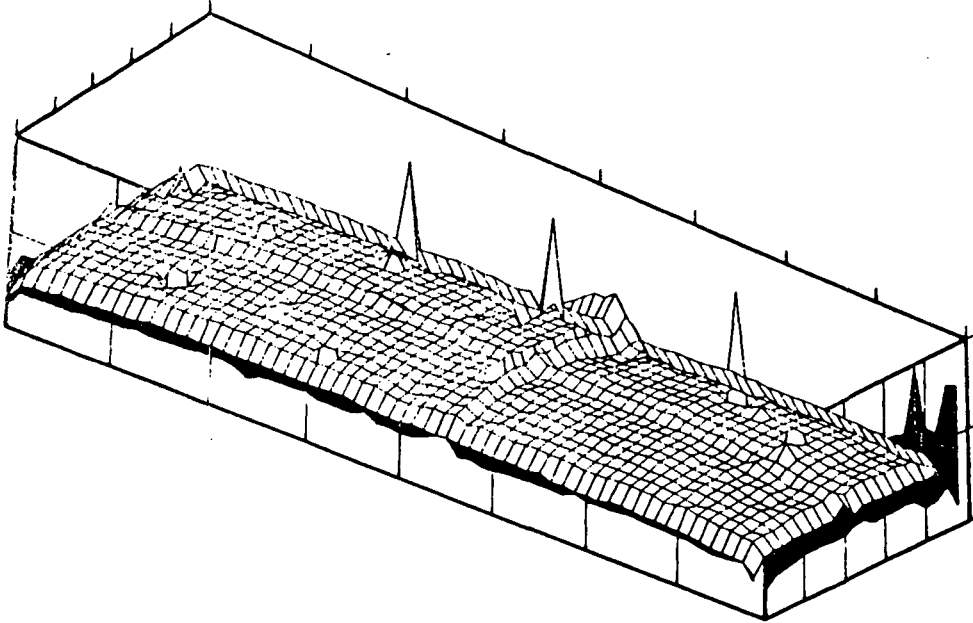
B. $\tau \gg 1 \text{ ms}$

(REPEAT)

FIND THE DARK FRAME VALUE FOR SEVERAL INTEGRATION TIMES

DARK FRAME ANALYSIS

- o **LOCATE A WELL BEHAVED REGION**
- o **READ NOISE VALUE IS FOUND @ SHORT INTEGRATION TIMES**

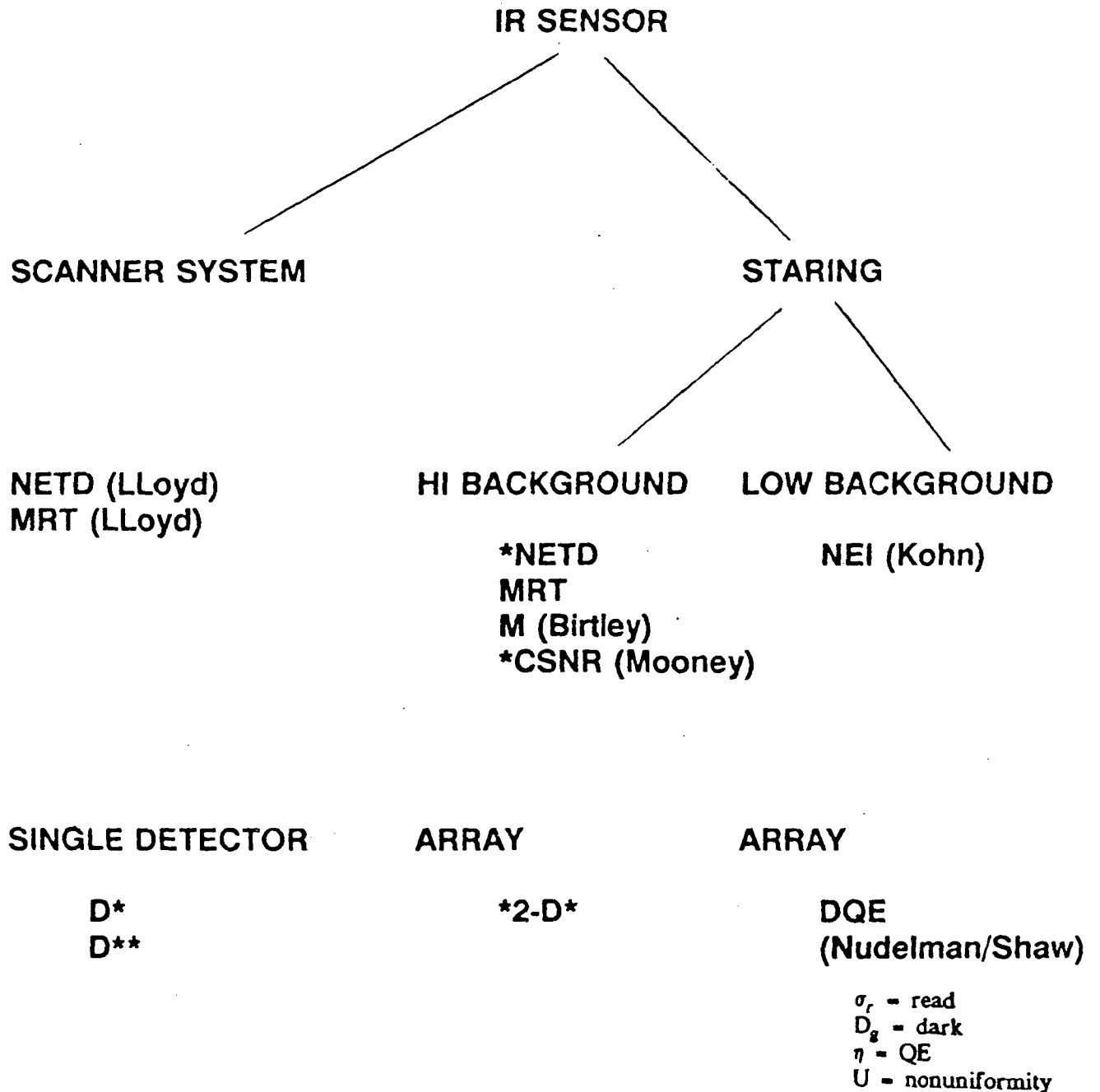


DARK CURRENT GENERATION RATE
 D_g (# OF e^- /SEC-PIXEL)

INCLUDES OTHER SOURCES

- o **LIGHT LEAKS**
- o **"SELF-EMISSION" OF ELECTRICAL COMPONENTS**

FIGURES OF MERIT



ARRAY TESTING AND FIGURE OF MERIT ARE APPLICATION DEPENDENT

* RELATED

NON-UNIFORMITY DEFINITION

$$\begin{aligned}
 U(E_p) &= \frac{\text{r.m.s. SPATIAL VARIATION IN ARRAY OUTPUT}}{\text{SPATIALLY AVERAGED ARRAY OUTPUT}} \\
 &= \frac{\sigma_{\bar{P}_{ij}}}{\langle \bar{P} \rangle}
 \end{aligned}$$

SPATIAL AVERAGE

$$\langle \bar{P} \rangle = \frac{1}{NM} \sum_i^N \sum_j^N \bar{P}_{ij}$$

SPATIAL VARIANCE

$$\sigma_{\bar{P}_{ij}}^2 = \frac{1}{NM} \sum_i^N \sum_j^N [\bar{P}_{ij} - \langle \bar{P} \rangle]^2$$

- o U (Ep) CAN BE IMPROVED THROUGH USE OF A NON-UNIFORMITY CORRECTOR
- o U (Ep) IS TYPICALLY REDUCED TO ZERO AT SYSTEM CALIBRATION POINTS.

ARRAY FIGURE OF MERIT

- o 2-D* IS A D* PLUS THE RANDOM CONTRIBUTION OF NON-UNIFORMITY, READ NOISE, AND DARK CURRENT
- o A MODIFIED D* CALLED 2-D* MAY BE USED IN LLOYDS NETD EXPRESSION TO YIELD CSNR

$$2 - D^* = \frac{\lambda}{hc} \sqrt{\frac{\eta}{2 \left[E_p + \frac{\sigma_r^2}{A_d \eta} + E_p^2 A_d \eta U^2 + \frac{D_g}{A_d \eta} \right]}}$$

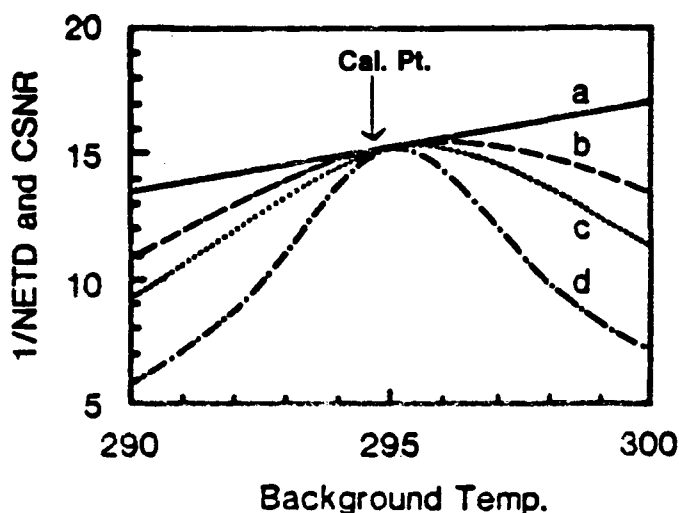
- o PHOTON SHOT NOISE - Ep
- o READ NOISE - σ_r
- o SPATIAL PATTERN - u
- o DARK CURRENT GENERATION (ZERO) - Dg

HIGH BACKGROUND CONTRAST SIGNAL-TO-NOISE RATIO (CSNR)

$$\text{CSNR} = \frac{\partial[E_p \eta A_d \tau] / \partial T}{[E_p \eta A_d \tau + \sigma_r^2 + E_p^2 \eta^2 A_d^2 U^2 \tau^2]^{1/2}}$$

E_p = PHOTON IRRADIANCE (P/s-cm²)
 η = QUANTUM EFF.
 A_d = PIXEL AREA
 τ = INTEGRATION TIME
 σ_r = READ NOISE
 U = RMS NON-UNIFORMITY
 T = TEMPERATURE

CSNR vs BACKGROUND TEMPERATURE FOR VARIOUS AMOUNTS OF RESIDUAL NON-UNIFORMITY



- a. NO NON-UNIFORMITY; $CSNR = 1/NETD$
- b. $u = 1\%$
- c. $> b$
- d. $> c$

**UNIFORMITY CORRECTION IS LIMITED BY
QUANTIZATION NOISE OF A/D CONVERTER**

**ARRAY TESTING IS APPLICATION DEPENDENT
THEREFORE, FIGURES OF MERITS VARY**

o HIGH BACKGROUND SENSOR SYSTEM

NETD - NOISE EQUIV. TEMP. DIFFERENCE

MRT - MINIMUM RESOLVABLE TEMPERATURE

CSNR - CONTRAST SIGNAL-TO-NOISE RATIO

o LOW BACKGROUND SENSOR SYSTEM

NEI - NOISE EQUIV. IRRADIANCE [PHOTONS/SEC-CM²]

DQE - DETECTIVE QUANTUM EFFICIENCY

Detective Quantum Efficiency - DQE (single detector)

$$\text{DQE} \equiv \frac{(S/N)_{\text{meas}}^2}{(S/N)_{\text{in}}^2} \quad \text{iff BLIP; } \eta$$

Apply to a 2-dimensional array

$$(S/N)_{\text{in}} = \sqrt{E_p A_d \tau}$$

$$(S/N)_{\text{meas}} = \frac{E_p A_d \tau \eta}{[E_p A_d \tau \eta + \sigma_r^2 + (E_p A_d \tau U)^2 + D_g \tau]^{1/2}}$$

↑
shot

↑
read

↑
uniformity

↑
dark
generation

2-Dimensional DQE

$$2\text{-DQE} = \frac{(S/N)_{\text{meas}}^2}{(S/N)_{\text{in}}^2} = \frac{1}{\frac{1}{\eta} + \frac{\sigma_r^2}{E_p A_d \eta^2 \tau} + E_p A_d \tau U^2 + \frac{D_g}{E_p A_d \eta^2}}$$

iff E_p is large enough to produce shot noise,
or U , σ_r , and D_g are small,
DQE is equal to quantum efficiency.

SAMPLE CALCULATION

$$\eta = 0.6$$

$$N_{\text{full}} = 10^6$$

$$A_d = (50 \mu\text{m})^2$$

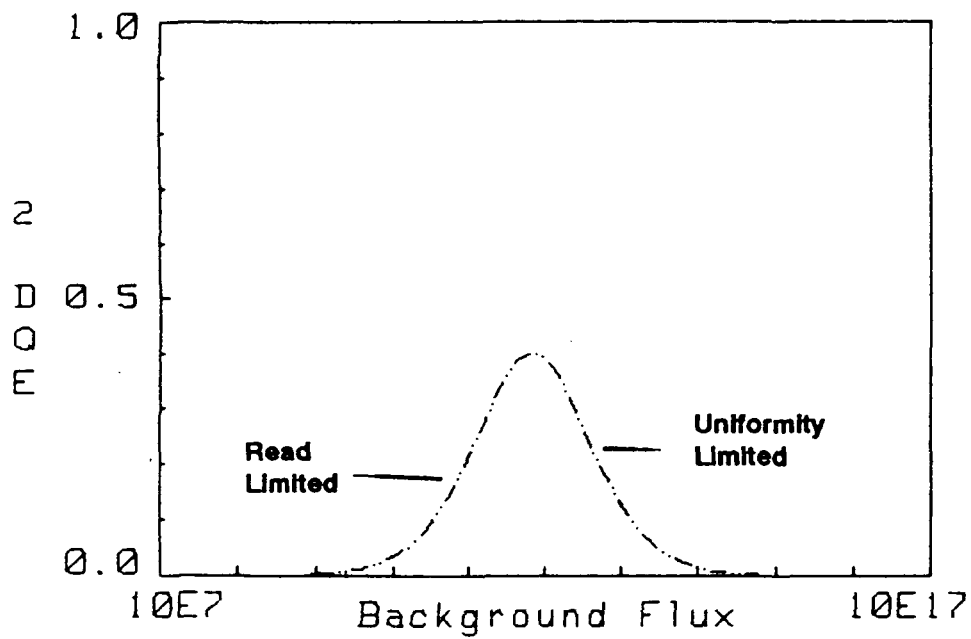
$$\tau = 0.001 \text{ sec}$$

$$\sigma_r = 50 e^-$$

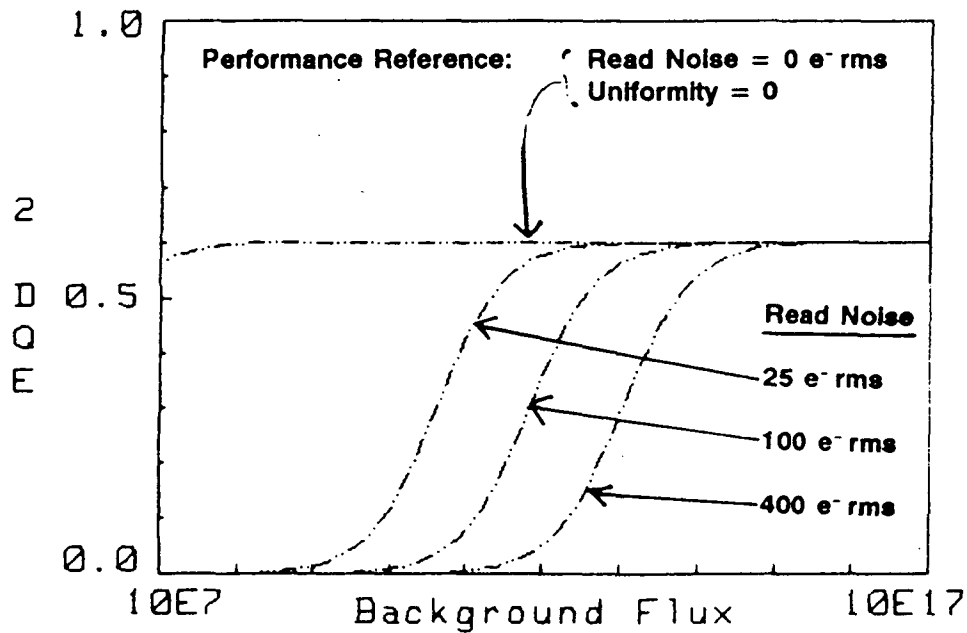
$$D_g = 10e^-/\text{sec-pixel}$$

$$U = 0.005$$

$$2 - \text{DQE} = 1 / \left(\frac{1}{0.6} + \frac{2.79(10^{11})}{E_p} + E_p \cdot 6.25(10^{-13}) + \frac{1.11(10^6)}{E_p} \right)$$

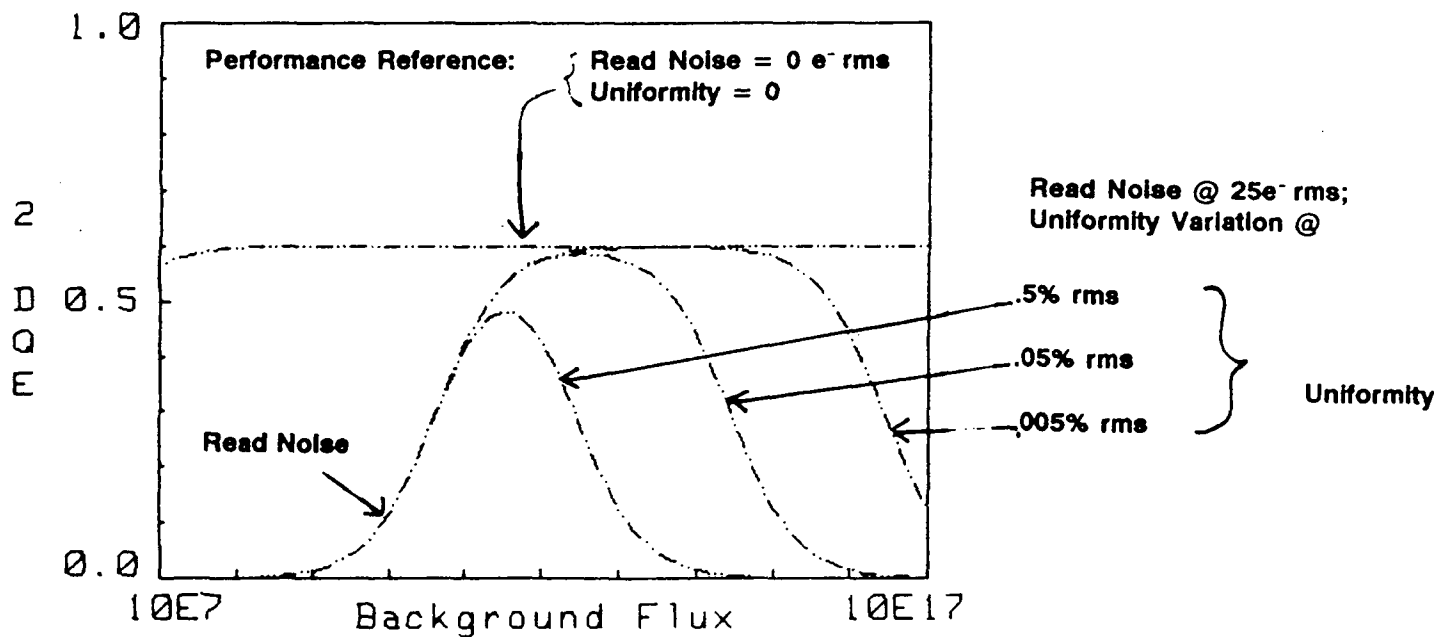


READ NOISE INFLUENCE



η = .60
 τ = .001 sec
 A_d = $(50\mu\text{m})^2$
 D_g = $10\text{e}^-/\text{sec-pixel}$

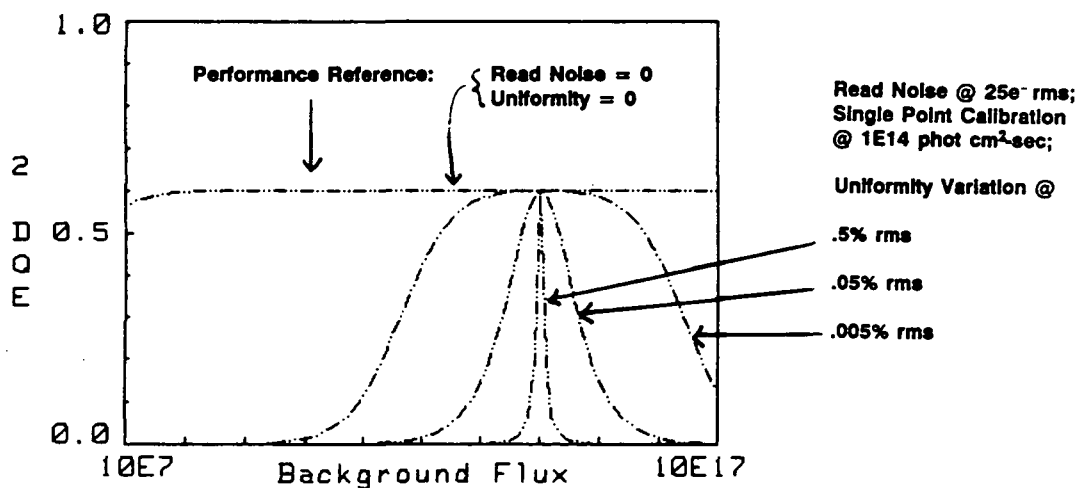
NON-UNIFORMITY INFLUENCE



WHERE DOES SPATIAL NON-UNIFORMITY COME FROM

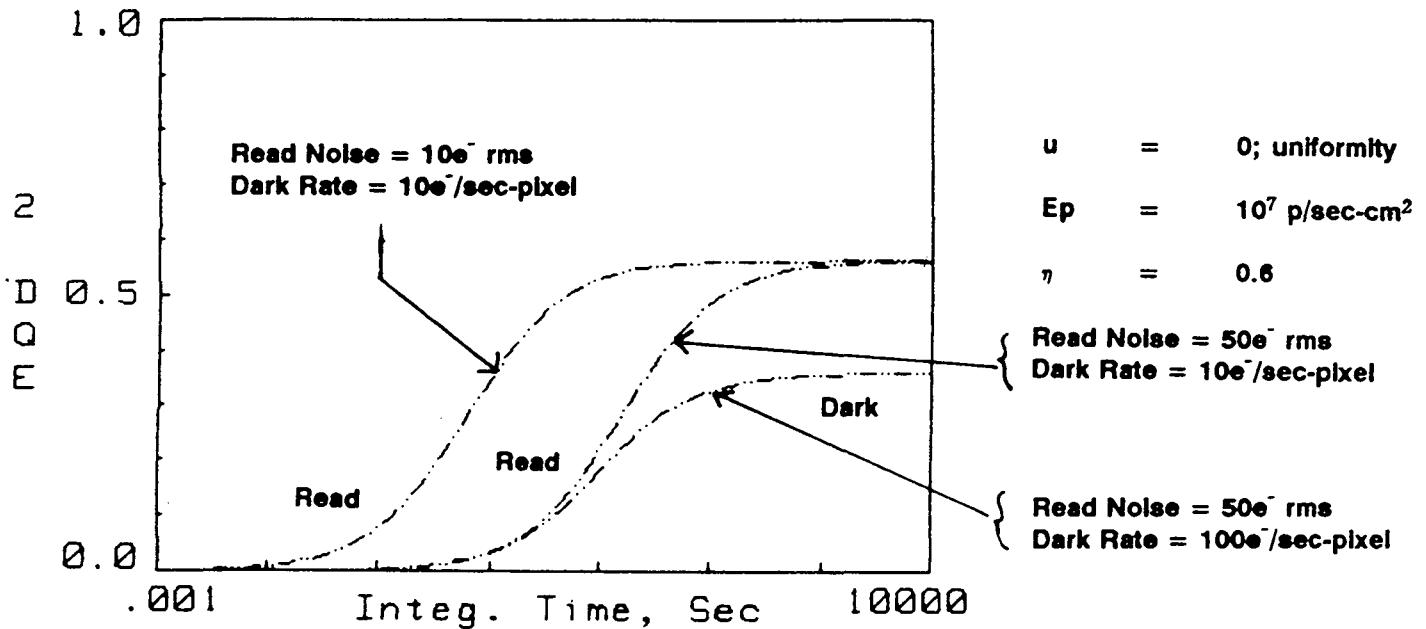
- o VARIATIONS IN DARK CURRENT DENSITY
- o VARIATIONS IN DETECTOR ACTIVE AREA
- o VARIATIONS IN THE ABSOLUTE VALUE, OR IN SOME CASES, VARIATIONS IN THE SPECTRAL SHAPE, OF THE QUANTUM EFFICIENCY CURVE.
- o VARIATIONS IN THE DETECTOR-TO-DETECTOR NON-LINEARITY OF RESPONSE
- o VARIATIONS IN THE $1/f$ NOISE ASSOCIATED WITH EACH DETECTOR OR OTHER UNIT-CELL ELECTRONICS.

FLAT FIELD CALIBRATION EFFECTS



DARK CURRENT EFFECTS

$$2 - DQE = \frac{1}{\frac{1}{0.6} + \frac{27.7}{\tau} + 1.1(10^{-2})D_g}$$



DARK CURRENT SIMPLY LIMITS THE MAXIMUM DETECTIVE QUANTUM EFFICIENCY

- o GOOD (↑) DQE REQUIRES "LOW" READ NOISE AND "LOW" DARK CURRENT

CONCLUSIONS

TESTS ON ARRAYS

- o **MEAN VARIANCE**
- o **DARK CURRENT GENERATION FRAMES**
- o **SIGNAL MEASUREMENTS FOR Q.E. VALUES**
- o **EFFECTIVE DETECTOR AREA**

FIGURES OF MERITS FOR FPA

- o **2-D* (CSNR - CONTRAST SIGNAL TO NOISE) RATIO**
 - **GOOD FOR HIGH BACKGROUNDS AND CALIBRATION ONCE AN HOUR**
- o **DQE (DETECTIVE QUANTUM EFFICIENCY)**
 - **GOOD FOR LOW BACKGROUNDS**
 - **COMBINES READ NOISE, DARK CURRENT, QUANTUM EFFICIENCY AND NON-UNIFORMITY INTO ONE PARAMETER**